

Ex. 5

$$\sum_n \frac{\lg(1+n^3)}{2^n + n^2 + 3^n} (x-3)^n$$

$$\frac{a_{n+1}}{a_n} = \frac{\lg(1+(n+1)^3)}{2^{n+1} + (n+1)^2 + 3^{n+1}} \frac{2^n + n^2 + 3^n}{\lg(1+n^3)} \xrightarrow{n \rightarrow \infty} \frac{1}{3}$$

$$\Rightarrow R = 3$$

$$x = 6 \quad \sum_n \frac{\lg(1+n^3)}{2^n + n^2 + 3^n} 3^n$$

$$\lim_{n \rightarrow \infty} b_n \neq 0 \Rightarrow \text{la s\u00e9rie ne converge pas}$$

$$x = 0 \quad \sum_n \frac{\lg(1+n^3)}{2^n + n^2 + 3^n} (-1)^n 3^n$$

$$\lim_{n \rightarrow \infty} c_n \neq 0 \Rightarrow \text{la s\u00e9rie ne converge pas}$$

\Rightarrow La s\u00e9rie converge absolument $\forall x \in]0, 6[$
et conditionnellement

La s\u00e9rie converge totalment $\forall x \in]0+\delta, 6-\delta]$ $0 < \delta < 3$