

⑥  $y e^{-2x^2} - 2x e^{-y} = f(x, y)$

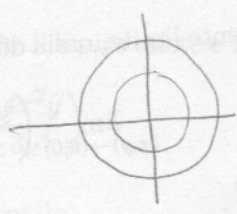
$x_0 = 1 \quad f(1, y) = 0 \quad y = 2 \quad g(1) = 2$

$\frac{\partial f}{\partial x} = y(-4x) e^{-2x^2} - 2 e^{-y}$

$\frac{\partial f}{\partial y} = e^{-2x^2} + 2x e^{-y} \quad \frac{\partial f}{\partial y}(1, 2) = e^{-2} + 2e^{-2} = 3e^{-2} \neq 0$

$g'(1) = - \frac{-8e^{-2} - 2e^{-2}}{3e^{-2}} = \frac{10}{3}$

⑦  $\iint_D \frac{|x|y}{x^2+y^2} dx dy$



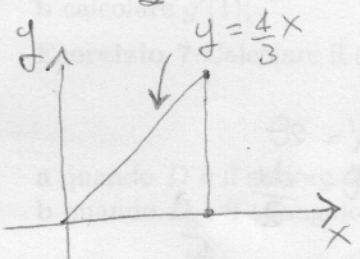
$\int_1^2 \int_0^{2\pi} \frac{\rho^2 |\cos\theta \sin\theta|}{\rho^2} \rho d\rho = \frac{1}{2} \rho^2 \Big|_1^2 \int_0^{2\pi} |\cos\theta \sin\theta| d\theta$

$= \frac{1}{2} (4-1) \int_{-\pi}^{\pi} |\cos\theta \sin\theta| d\theta = \frac{3}{2} \cdot 2 \int_0^{\pi} |\cos\theta \sin\theta| d\theta =$

$|\cos\theta \sin\theta| \text{ è pari} = 3 \int_0^{\pi} \sin\theta |\cos\theta| d\theta =$

$= 3 \left[ \int_0^{\pi/2} \sin\theta \cos\theta d\theta - \int_{\pi/2}^{\pi} \sin\theta (-\cos\theta) d\theta \right] = \frac{3}{2} \left[ \sin^2\theta \Big|_0^{\pi/2} - \sin^2\theta \Big|_{\pi/2}^{\pi} \right] =$

$= \frac{3}{2} \cdot 2 = 3 \quad \text{Oppure} \quad \int_0^{2\pi} |\cos\theta \sin\theta| d\theta = 4 \int_0^{\pi/2} \sin\theta \cos\theta d\theta =$



b)  $\iint_D \frac{|x|y}{x^2+y^2} dx dy = \int_0^3 \int_0^{4/3 x} \frac{x y}{x^2+y^2} dx dy =$

$= \int_0^3 x \left( \frac{1}{2} \lg(x^2+y^2) \Big|_0^{4/3 x} \right) dx = \frac{1}{2} \int_0^3 x \left[ \lg \frac{25}{9} x^2 - \lg x^2 \right] dx =$

$= \frac{1}{2} \int_0^3 x \lg \frac{25}{9} dx = \frac{1}{2} \lg \frac{25}{9} \cdot \frac{9}{2} = \frac{9}{4} \lg \frac{25}{9}$