

Cherenkov radiation of Josephson vortices and Cherenkov Josephson Microwave oscillators for submm range.

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Abstract

The report is devoted to theoretical development of the concept of Cherenkov radiation of Josephson vortices and experimental investigation of characteristics of Cherenkov Josephson FluxFlow oscillators with different designs.

Now it is well known that josephson vortex moving in josephson transmission line with dispersion can radiate electromagnetic wave when cherenkov condition of equality of soliton velocity to phase velocity of the wave is fulfilled [1]. The scheme of Cherenkov oscillator contains Long Josephson Junction (LLJ)(or array of LLJ) electro-dynamically built in some waveguide system which provides dispersion to make possible fulfilment of Cherenkov condition. This waveguide system may be simple strip line (even passive edges of LJ may take part of it), periodical inhomogeneous strip lines or dielectric wave guide system. Besides, the Cherenkov radiation of vortices is possible in 2D Josephson Junctions [2,3]. Due to volume nature of interaction between vortices and electromagnetic waves the use of Cherenkov radiation will help to improve characteristics of existing types of josephson oscillators i.e. expand their frequency range and output power, make narrower spectral width of radiation.

Cherenkov oscillators based on single 1D linear and annular LJ built in stripline with periodical varied width were experimentally tested. Some preliminary results regarding these designs of Cherenkov oscillators were published earlier [4,5].

IV curves for external magnetic field applied were measured and electromagnetic radiation at the frequency range 80-120 GHz were registered by the room-temperature receiver. The new band structure of Fiske steps corresponding to band spectrum of eigenmodes of periodical transmission line was found and strong radiation with frequency and bandwidth depending on biasing current was observed. Experimental results are in a good agreement with theoretical predictions and simulation. New design of Cherenkov oscillators based on parallel and series arrays of several LLJs integrated into the only stripline was suggested and preliminary experiments were carried out.

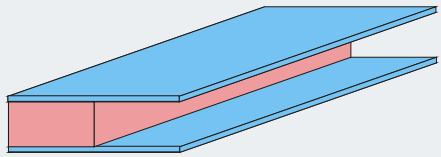
References

1. V.V. Kurin, A.V. Yulin, Radiation of Linear Waves by Solitons in a Josephson Transmission Line with Dispersion, Phys.Rev. B, 55, 9, 11659, 1997
2. V.V. Kurin, A.V. Yulin, I.A. Shereshevskii, and N.K. Vdovicheva, Cherenkov Radiation of Vortices in a Two-dimensional Annular Josephson junction, Phys.Rev.Lett., 75, 15, 2995, 1995
3. A. Wallraff, A. Ustinov, V. Kurin, I. Shereshevsky, N. Vdovicheva, Observation of whispering gallery resonances in annular Josephson junction, Phys.Rev.Lett., 85, 15, 3095, 2000
4. V. Kurin, A. Yulin, E. Goldobin, A. Klushin, H. Kolstedt, M. Levichev, and N. Thyssen, Experimental investigation of Cherenkov Flux Flow Oscillators, IEEE transaction on Applied Superconductivity, 9, 2, 3737, 1999
5. A.V. Baryshev, A.V. Yulin, V.V. Kurin, V.P. Koshelets, S.V. Shitov, A.V. Shchukin, P.N. Dmitriev, and L.V. Fillipenko, Design and Fabrication of Cherenkov FluxFlow Oscillator, IEEE transaction on Applied Superconductivity, 9, 2, 3737, 1999

Josephson Transmission Lines with Dispersion = Long Josephson Junction built in External wave-guide system

Examples of JTL's

Single LJJ in the Strip-line (SL)

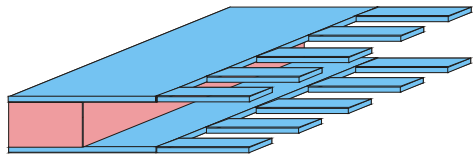


$$D(\omega, k) = -i\omega(-i\omega + \gamma) + k^2 + \alpha\kappa^2 \frac{\tanh \kappa W}{\kappa W}$$

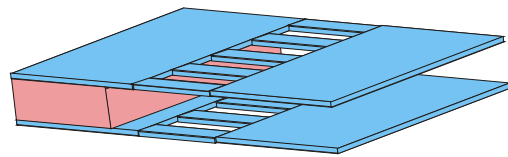
$$\kappa^2 = k^2 - \frac{\omega(\omega + i\Gamma)}{v^2}$$

$$\alpha = \frac{WL_J}{W_J L_{SL}} \quad \text{-Coupling parameter}$$

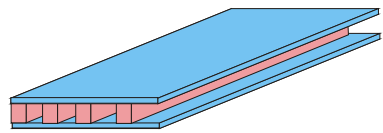
LJJ in the SL with side resonators



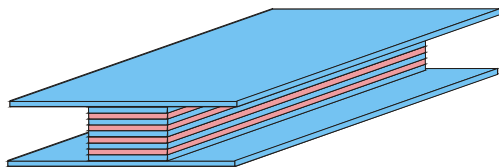
More complicated structure
with two Strip-Lines



Parallel LJJ array in SL



Josephson Superlattice in Strip-line



All system shown are two-dimensional and are described by 2-D Sine-Gordon equation

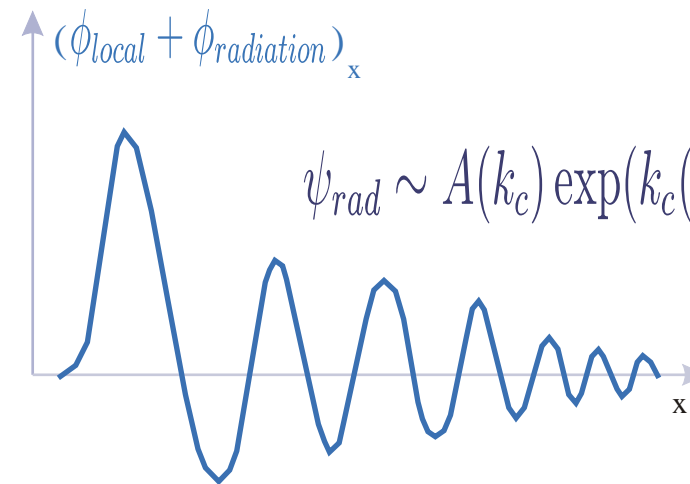
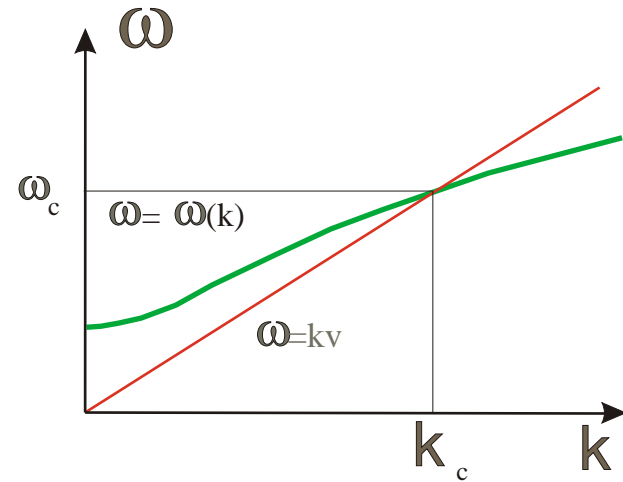
$$\frac{\Phi_0}{2\pi} \left\{ C(\vec{\rho}) \frac{\partial^2 \phi}{\partial t^2} + G(\vec{\rho}) \frac{\partial \phi}{\partial t} - \text{div} L^{-1}(\vec{\rho}) \nabla \phi \right\} + j_c(\vec{\rho}) \sin \phi = j_e$$

For narrow junction it may be reduced to 1D integral equation

$$\hat{D}\varphi + \sin \varphi = j_e,$$

Where \hat{D} -linear operator

Common feature of such a system -radiation of linear waves by moving vortices due to Cherenkov effect



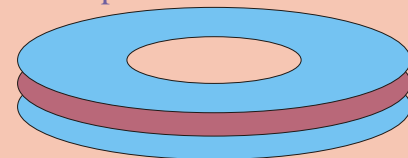
Tailed Solitons

$$\phi = \phi_{local} + \phi_{radiation}$$

$$\psi_{rad} \sim A(k_c) \exp(k_c(x - vt) + \Gamma(x - vt)/(v - v_g(k_c)))$$

results in:
long-range interaction and,
changing spectrum of vortex

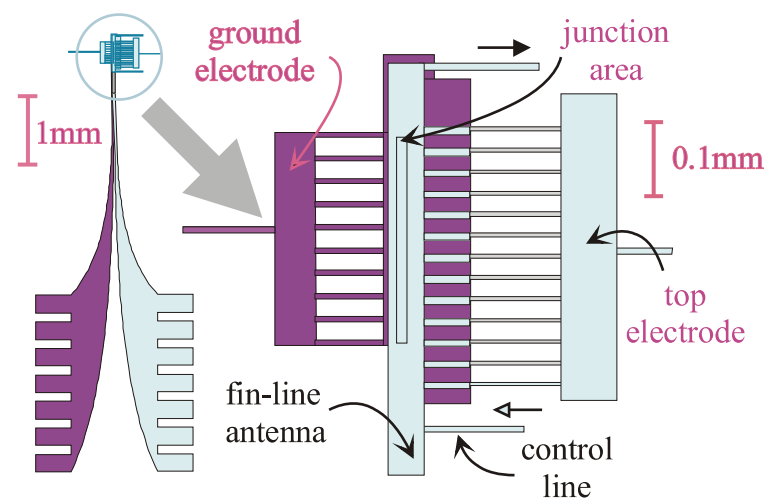
Annular Josephson Junction



$$\frac{\partial^2 \phi}{\partial t^2} + \gamma \frac{\partial \phi}{\partial t} - \frac{1}{r} \frac{\partial}{\partial r} r \frac{\partial \phi}{\partial r} - \frac{\partial^2 \phi}{\partial \theta^2} + \sin \phi = j_e$$

Experimental investigation of Long JJ built in space periodical slow-wave system

Appearance of the Sample



Parameters

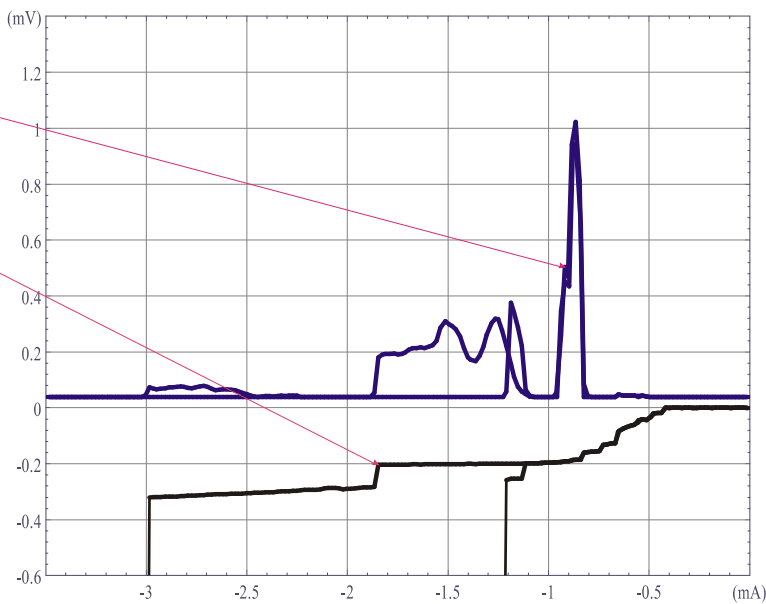
$L=1-2\text{ mm}$
 $j_c=400\text{A/cm}$
 $V=0.03c$
 $l_m=27\text{m}$

2

Receiver output

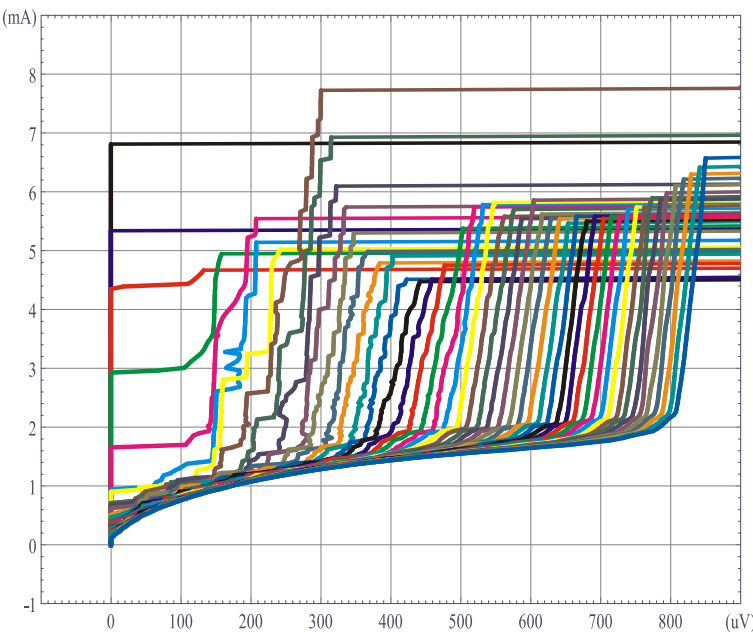
I-V curve

Intensity of radiation at 120GHz
vs biasing current



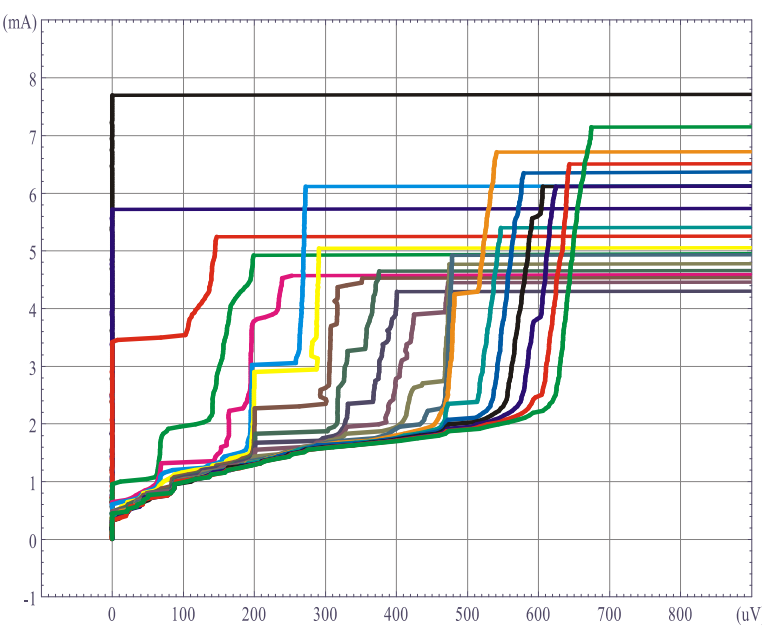
Set of I-V curves for test sample-
without external waveguide system

Usual Fiske structure is seen

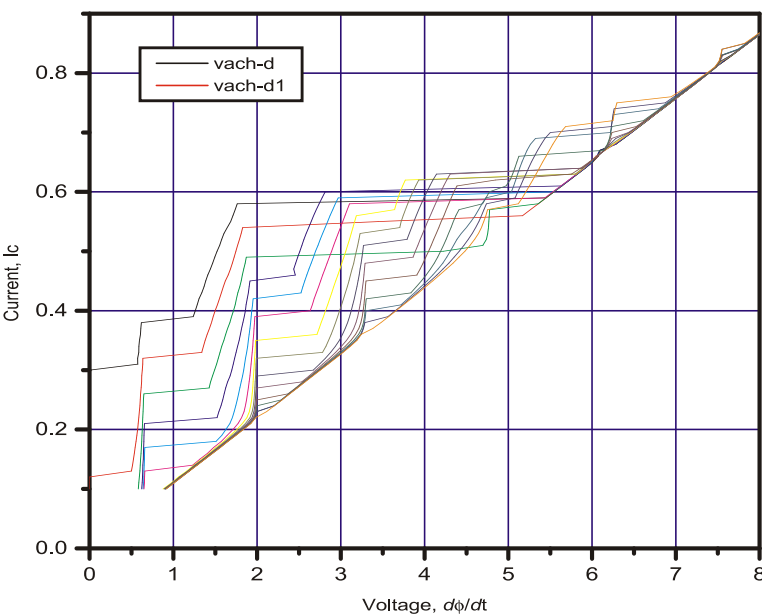


Set of I-V for LLJ coupled with
space-periodical slow-line

Quantity of steps is reduced
and band structure observable

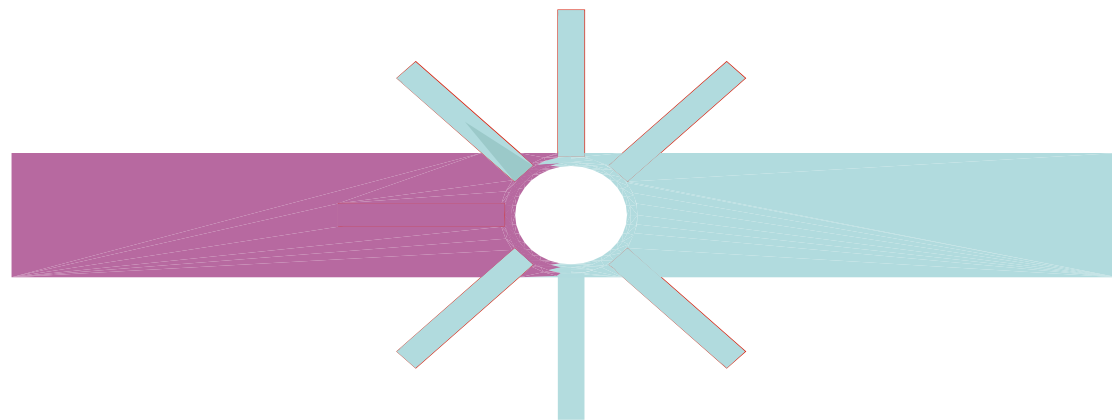


I-V simulated using
RSJ 1D approach



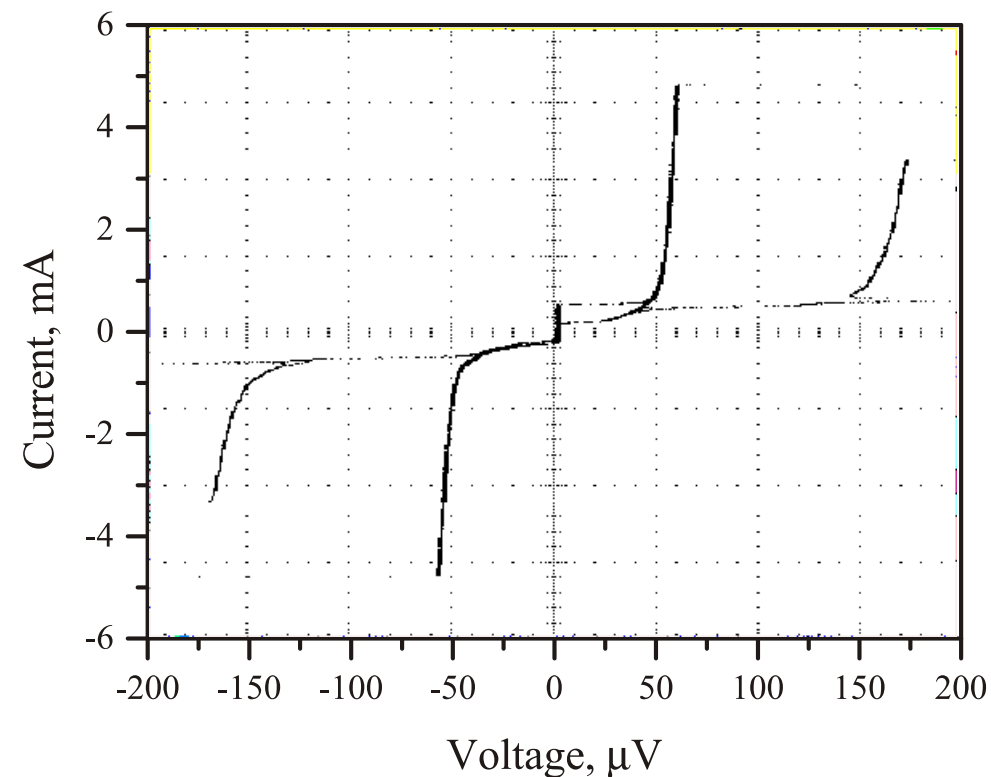
Cherenkov resonances in the annular JJ with space-periodical slow-line (experiment)

Samples with different number and length of stubs are tested



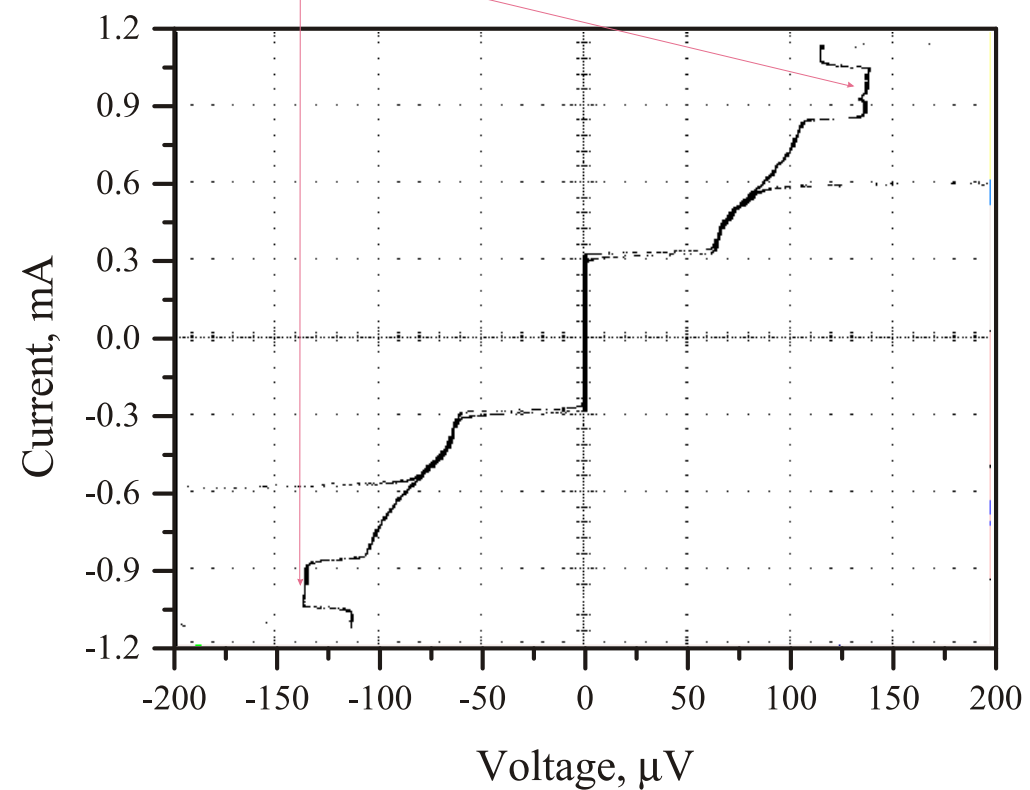
Test annular junction (no stubs)

Different branches correspond to $N=1,2$ trapped fluxons

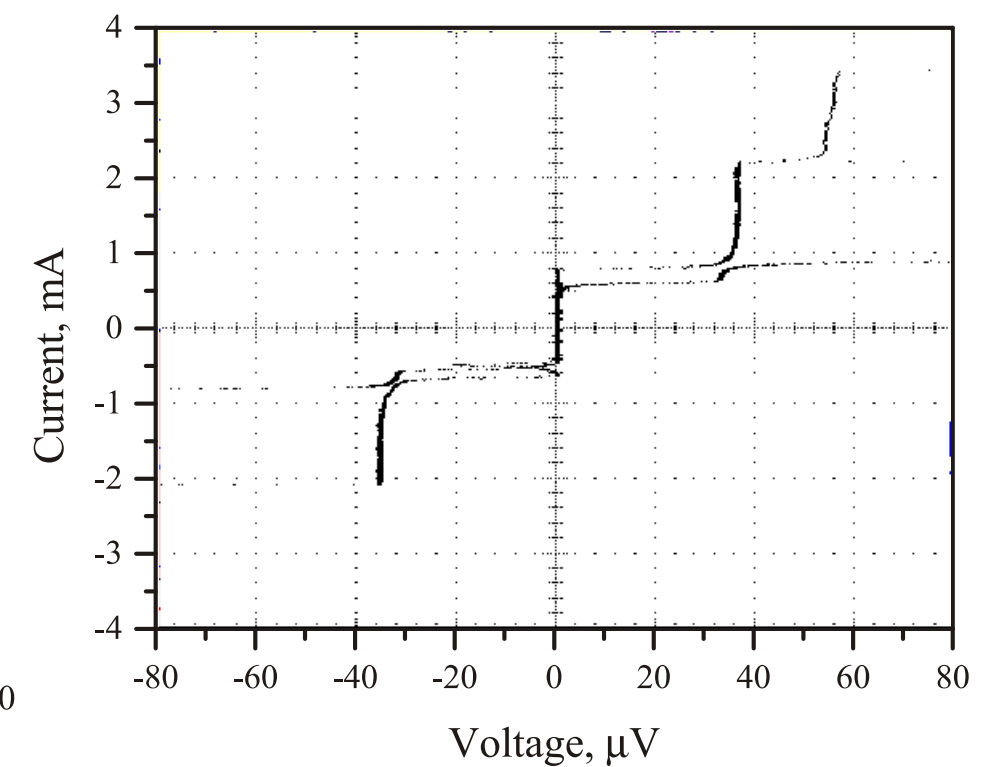
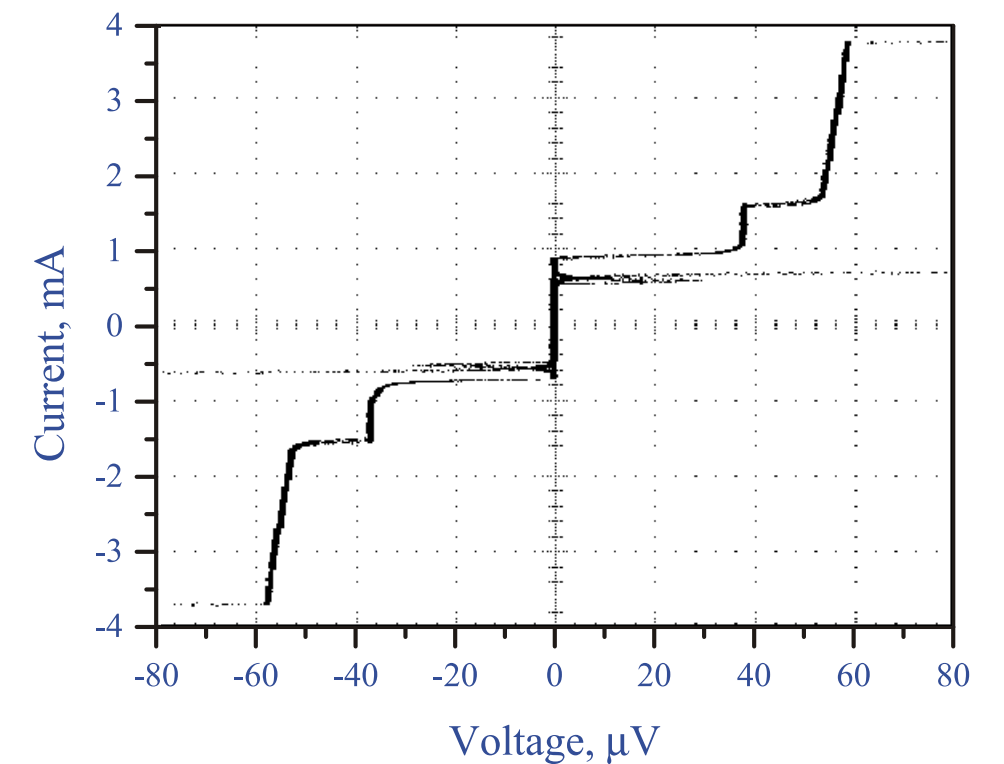


I-V for two fluxons trapped

resonance steps



IV Steps for two temperatures,
one fluxon trapped

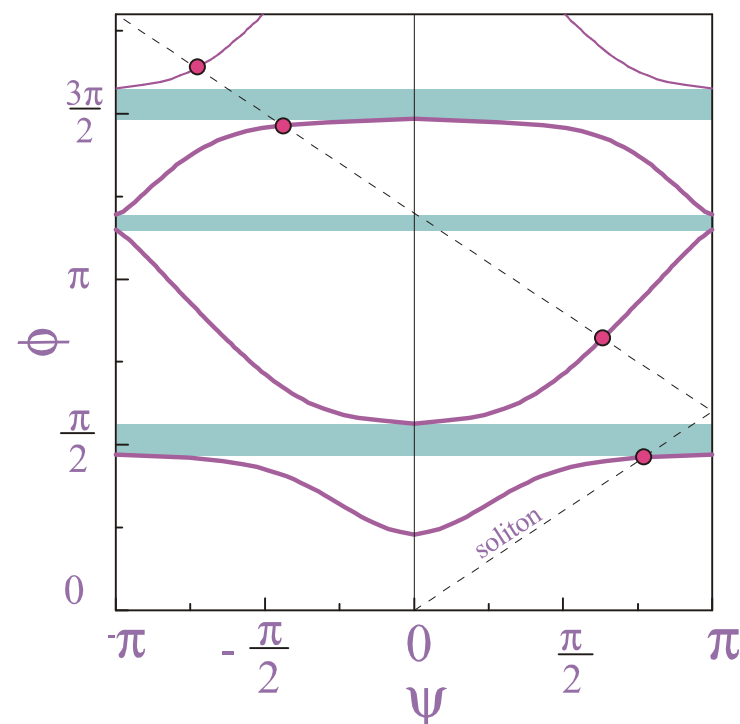


Cherenkov resonances in the annular JJ with space-periodical slow-line (theory+simulation)

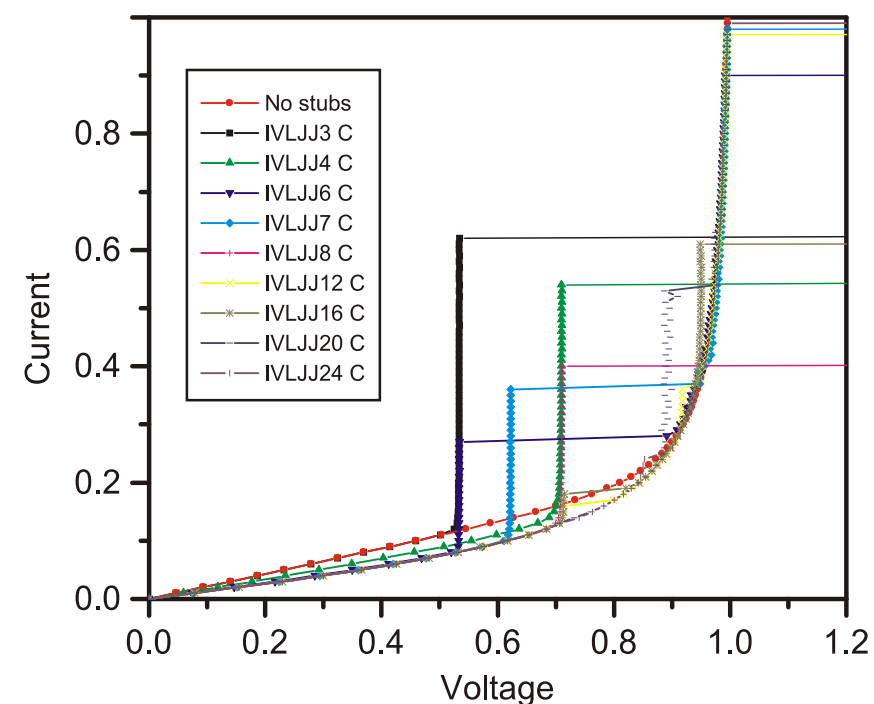
Theory and experiment for Cherenkov effect in smooth wide annular junctions

1. A. Wallraff, A. Ustinov, V. Kurin, I. Shereshevsky, N. Vdovicheva, Whispering Vortices, Phys.Rev.Lett., v.84, n.1, 151, (2000)
2. V. Kurin, A. Yulin, I. Shereshevskii, and N. Vdovicheva, Cherenkov Radiation of Vortices in a Two-dimensional Annular Josephson junction, Phys.Rev.Lett, 80, 15, 3372, 1998

Dispersion of linear waves in space periodical line,
red points-position of Cherenkov resonances

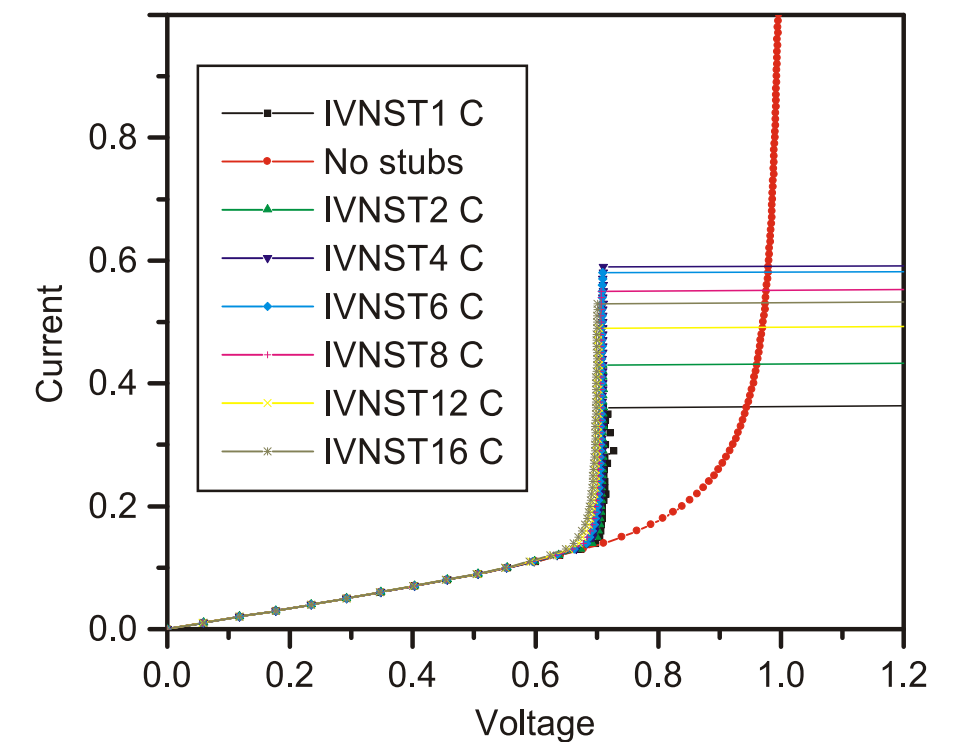


Different JJ length

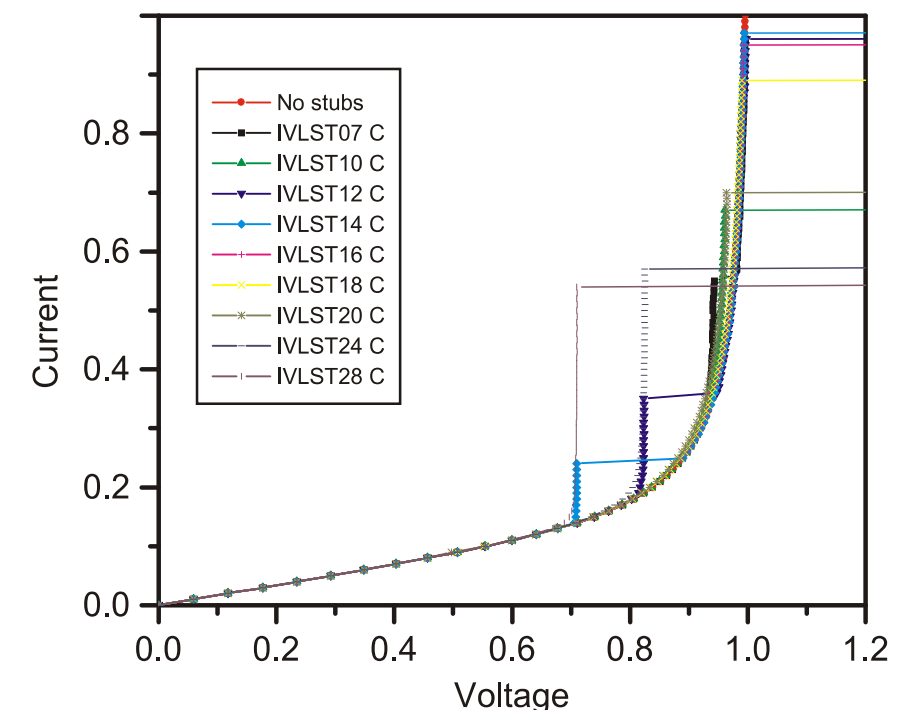


Steps for annular JJ

with different number of stubs,
one fluxon in JJ



Different stub length



Josephson Superlattice built-in Strip-Line

Equations $i=1..N$

$$j_{it}j_{it}+j_{it}(x)\sin= G_{ixx} \hat{U}_i \hat{a} j_i + j_{ext}$$

G-linear operator of external impedance, originated from SL

$$\hat{U} = \int_{-\infty}^{\infty} \hat{G}(k) e^{-i\omega t + i k x} dk$$
$$\hat{G} = \frac{1}{2\pi} \int_{-\infty}^{\infty} \hat{G}(k) e^{-i\omega t + i k x} dk$$

For smooth SL

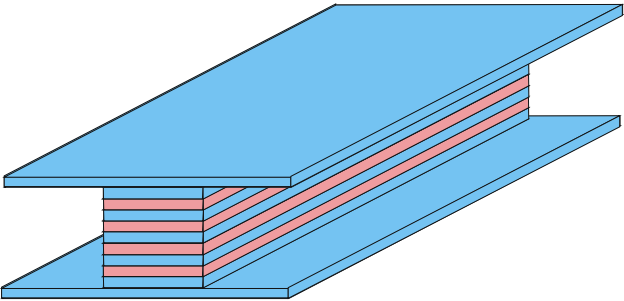
$$G(w,k) = (a/w)(k^2 - w(w + iG)/v^2) \tanh(k^2 - w(w + iG)/v^2) w$$

a-coupling, w-width of SL,
v-dimensionless wave velocity in SL

Stability of Symmetric Flux-Flow
on condition that

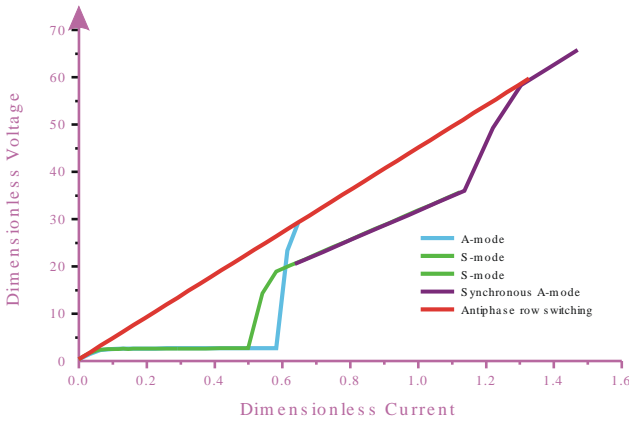
$$b_a = (1 - u^2/v^2)/(1 - u^2) < 0$$

where u is vortex velocity,
lying in the range $-v < u < v$,
 $v = (1 + \dots)/(1 - a^2/v^2)$ - velocity of fully
symmetric mode



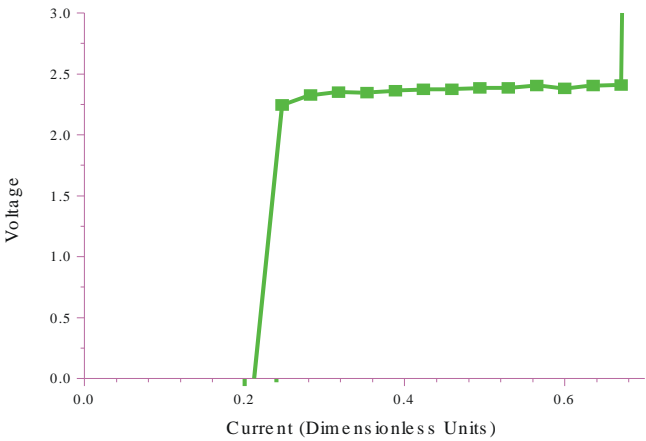
Computer Simulation for $N=2$
subSwihart SL, $v=0.9$,
 $a=2$, $w=0.2$
periodical boundary condition,
two trapped vortices

I-V curves for different dynamic states



Stack with artificial
commensurable pinning,

jump from superconducting
to flux-flow symmetric state



Flux-Flow branches zoomed

