

Teoria dei Sistemi: written exam of january 13th, 2014



Nyquist Formula:  $p_{CL} = p_{OL} - N$ 

where:

 $p_{ot}$ : number of poles with positive real part of the **open loop** transfer function W(s) $p_{ct}$ : number of poles with positive real part of the **closed loop** transfer function W(s)/(1+W(s))N counts the number of encirclement of the point -1+j0 made by the graph of  $W(j\omega)$ N positive for counterclockwise encirclements

In the problem,  $p_{CL} = 2$ .

For K > 0 we have N=0, and therefore  $p_{cL}=2$  (instability of the closed loop system) For  $K \in (-0.1,0)$  we have N=0, and therefore  $p_{cL}=2$  (instability of the closed loop system) For K < -0.1 we have N=1, and therefore  $p_{cL}=1$  (instability of the closed loop system) Thus, the closed loop system is unstable for any feedback gain K.